

**COE CST Third Annual
Technical Meeting:
Fracture Mechanics of
Sapphire for High
Temperature Pressure
Transducers
William Oates**

Date of Presentation



Overview

- Team Members
- Motivation
- Background
 - Structure property relations
- Experimental Work
 - SEM Characterization
 - TEM Characterization
- Modeling
 - Coupling dislocation evolution with fracture mechanics
- Summary and future work
- Contact Information

Team Members

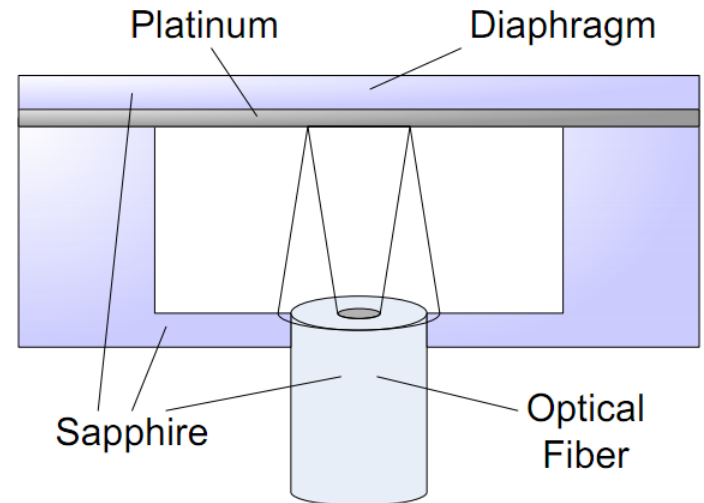
- Mark Sheplak (UF)
- Justin Collins (FSU), David Mills (UF), Daniel Blood (UF), Tony Smitz (UNC Charlotte)

Motivation

- Commercial sensors capable of up to approximately 600°C
 - Uses SOI technology
- Alternative material sapphire: potentially capable of up to 1500°C
- Laser machining to cut specimens
 - Hard
 - Chemically Inert



Kulite Pressure Transducer

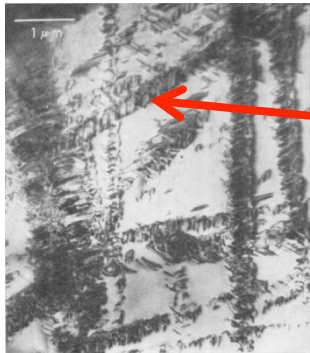


Structure-Property Relations

- Sapphire crystallographic structure
 - Complicated by hexagonal cage & internal rhombohedral structure
- *Anisotropic elastic behavior
 - Rhombohedral—not hexagonal

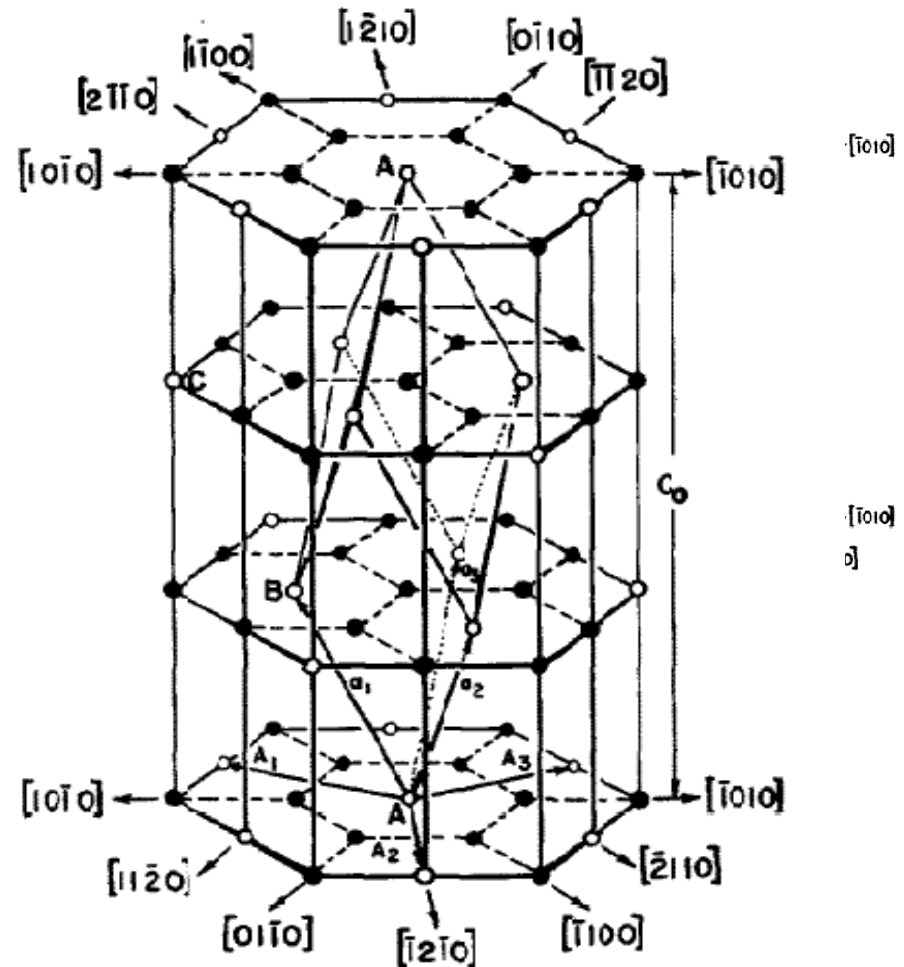
$$\sigma_{ij} = C_{ijkl} \epsilon_{kl}$$

- Melting temperature 2030 °C



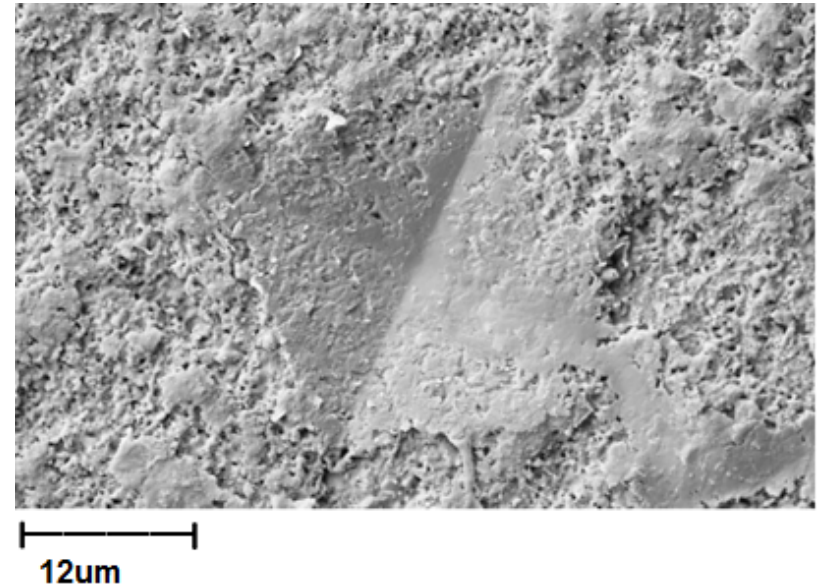
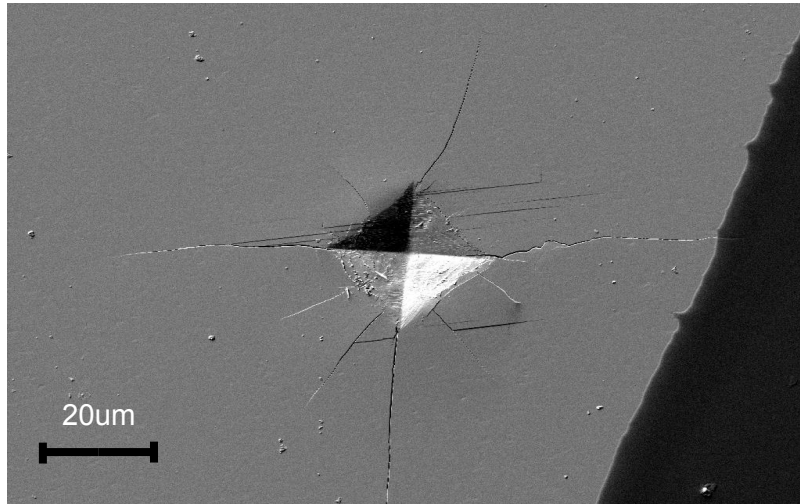
Basal half loop dislocation

Hockey, Journal of the American Ceramic Society, May 1971, Vol. 54, No. 5



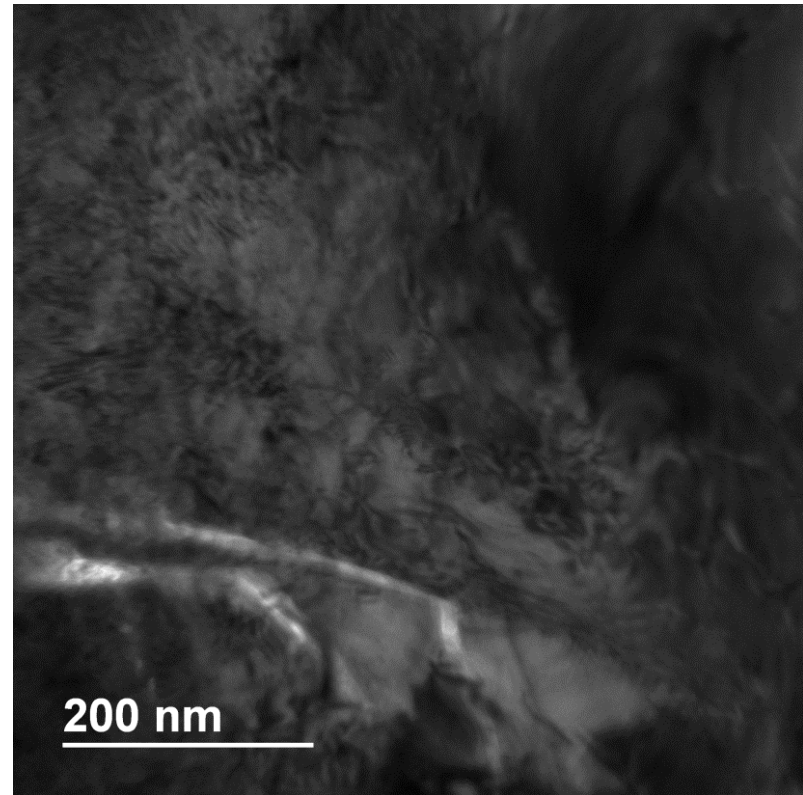
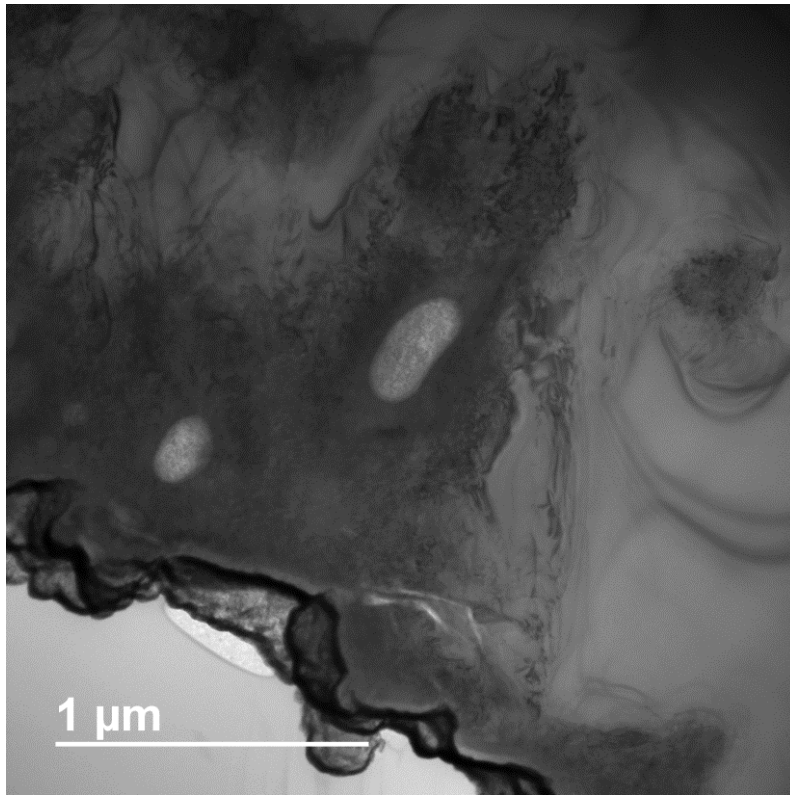
Toughness Induced Laser Machining

- Vicker's indentation characterization
- No visible cracks in laser machined specimens
- Laser machining parameters
 - 10 kHz rep rate, 10 mm/s scanning speed, 3.8 J/cm² fluence, 3μm stepover



TEM Characterization

- High resolution TEM located at the NHMFL
 - 0.8 Angstrom resolution



Coupling Dislocation Theory and Solid Mechanics

Linear Momentum Balance

PDE Governing Dislocation Mechanics

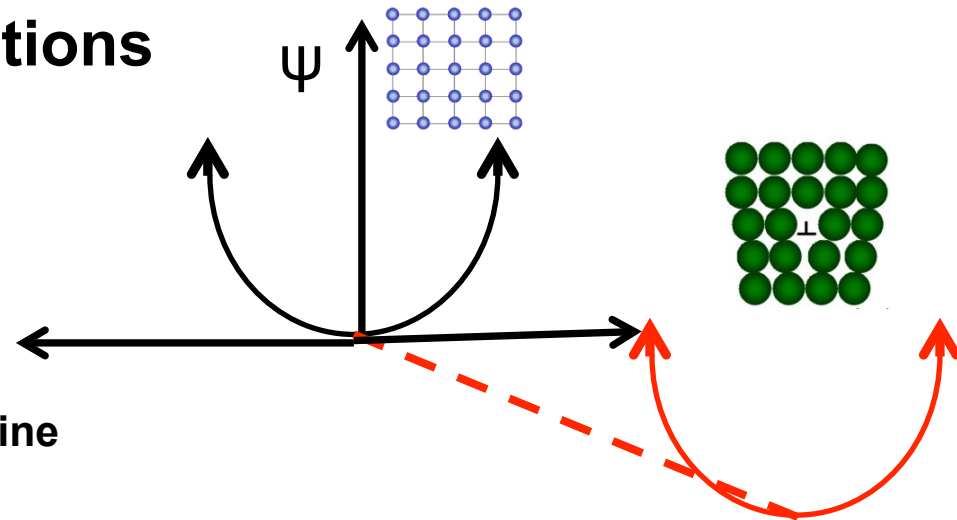
Energy to formulate dislocations

=

Where

Single Crystal

Polycrystalline



FEM Model of Single and Polycrystalline

Polycrystalline



Single crystalline



Fracture Analysis

Stroh's Formalism

Equilibrium

Constitutive Relation

Boundary Condition

Generalized Displacement
Potential

J-Integral

Eshelby stress tensor

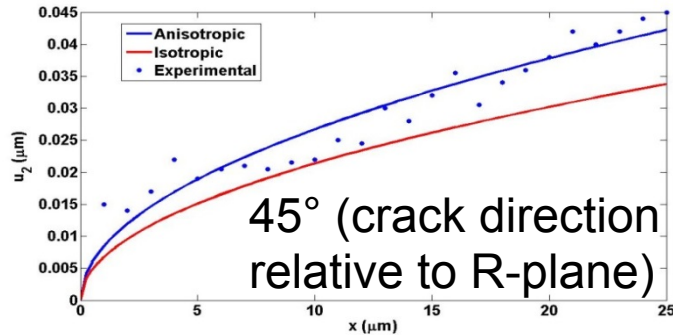
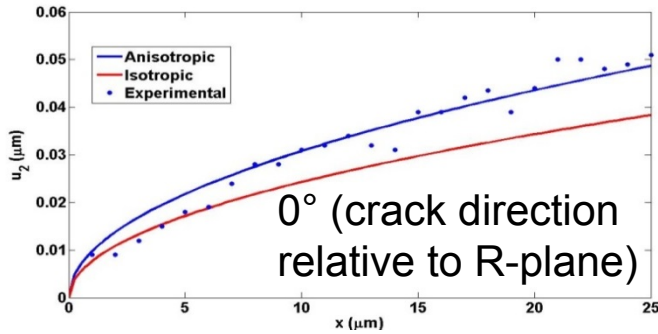
J_1 (direction of the crack)

=

When this condition occurs a
crack propagates.

Comparison of Fracture Toughness

Experimental



$$K_{1c} \cong 2.2 \text{ MPa} \cdot \text{m}^{1/2}$$

$$J_{Ic} \cong 11.64 \text{ N/m}$$

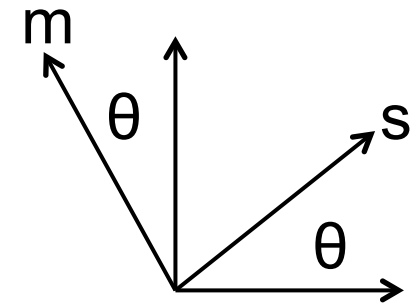
$$K_{1c} \cong 2.50$$

$$\cong 15.25$$

Simulation

Crack Tip Driving Force Comparison, J^*

$\Theta=0$	$\Theta=45$
20.9 N/m	18.84 N/m



Summary

- Laser machining subsurface damage quantified
 - TEM characterization identified dislocations
- Dislocations modeling coupled with solid mechanics
 - Changes in slip system cause change in the crack tip driving force.
- Future work
 - Comparison of slip systems in Sapphire for 3D model.
 - Thermal annealing & laser parameter studies

Acknowledgements

- National High Magnetic Field Laboratory
 - Dr. Yan Xin
 - NHMFL-Applied Superconductivity Center
- FCAAP
- FAA
- FAMU-FSU College of Engineering
- University of Florida
 - Mark Sheplak, David Mills, Daniel Blood, Tony Smitz (UNC Charlotte)

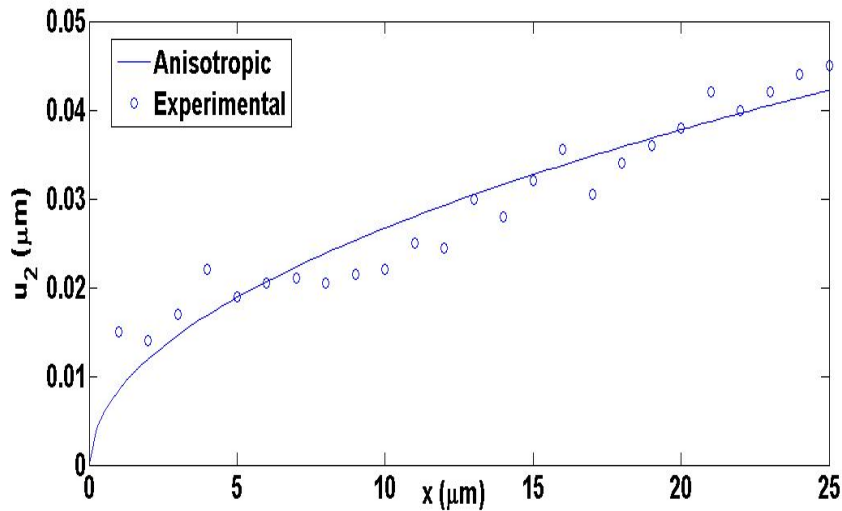
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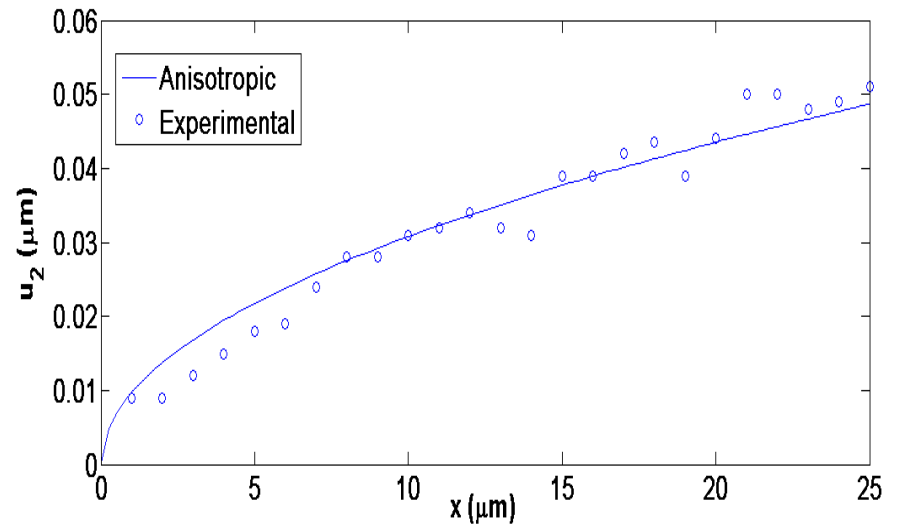
Fracture Toughness

- $K_{1c} \cong 2.2 \text{ MPa}\cdot\text{m}^{1/2}$
- $J_{Ic} \cong 11.64 \text{ N/m}$

- $K_{1c} \cong 2.50$
- $\cong 15.25$

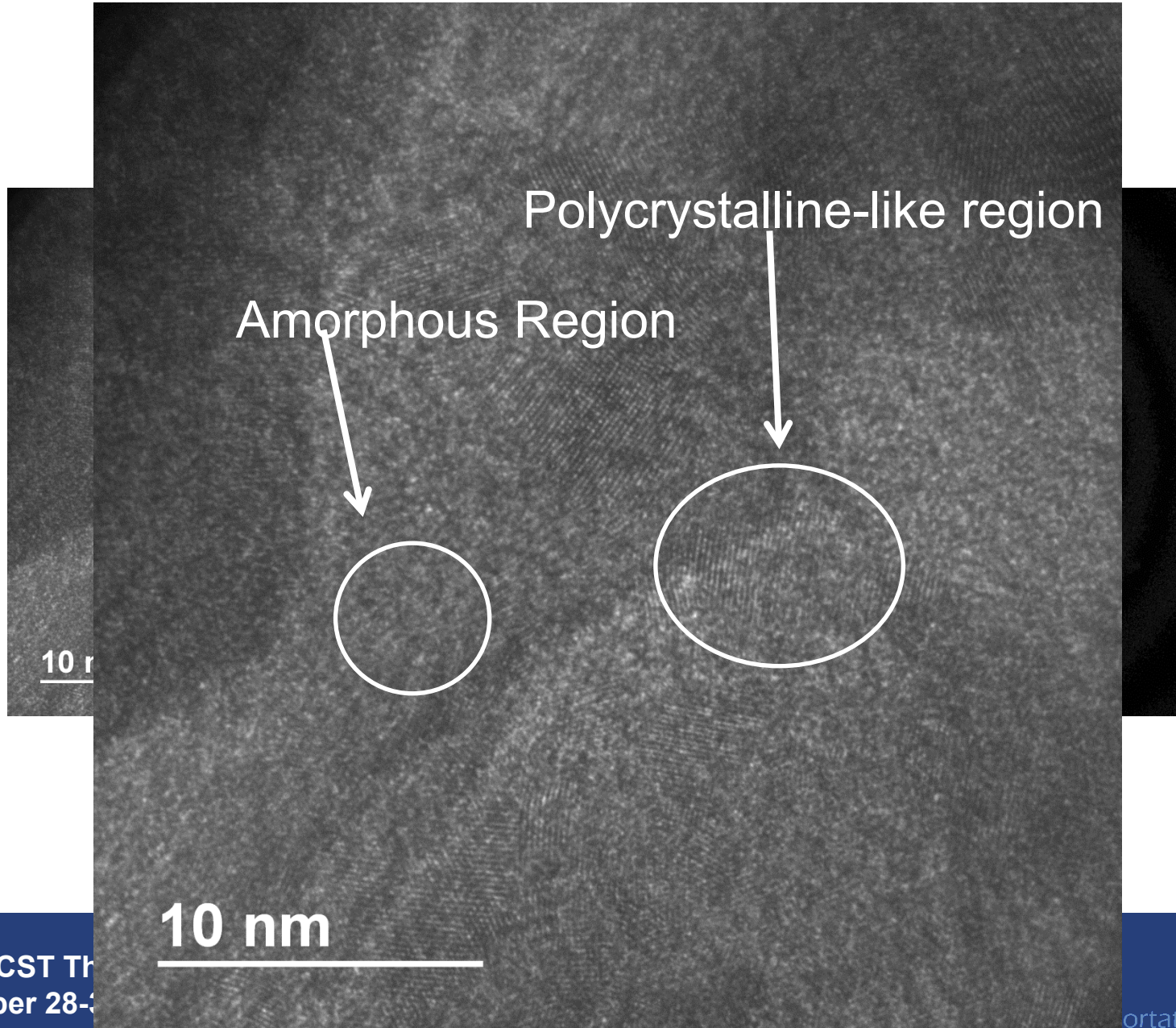


Indentation at $\sim 0^\circ$



Indentation at $\sim 45^\circ$

TEM Characterization-2



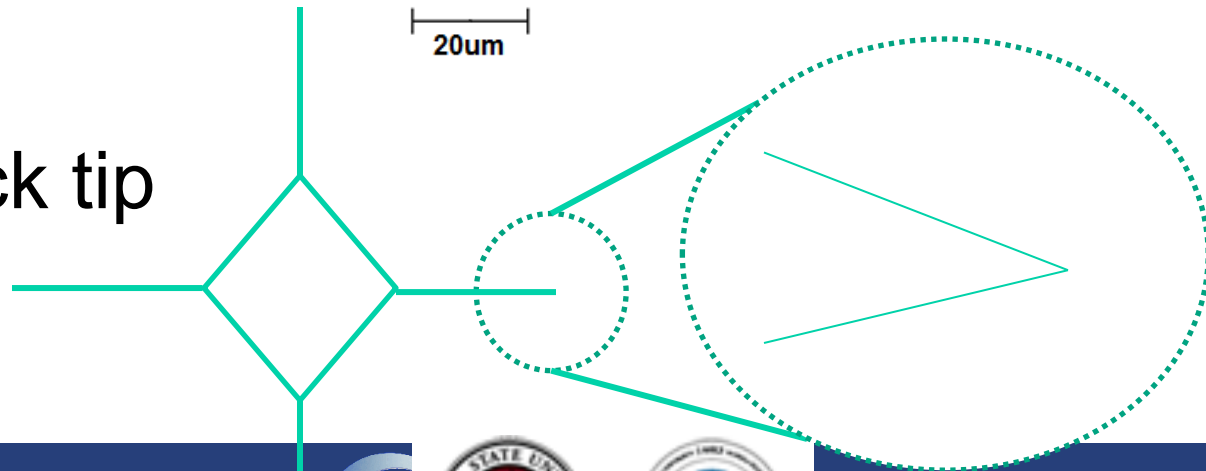
Anisotropic Fracture Stroh's Formalism

- Equilibrium
 - $\nabla \cdot \sigma = 0$
- Constitutive Relation
 - $\sigma_{ij} = C_{ijkl} \epsilon_{kl}$
- Boundary Condition
 - $t_i = \sigma_{ij} n_j$
- Generalized Displacement Potential
 - $u_i = 2 \sum_{j=1}^3 \text{Re} \{ A_{ij} f(z_j) q_j \}$



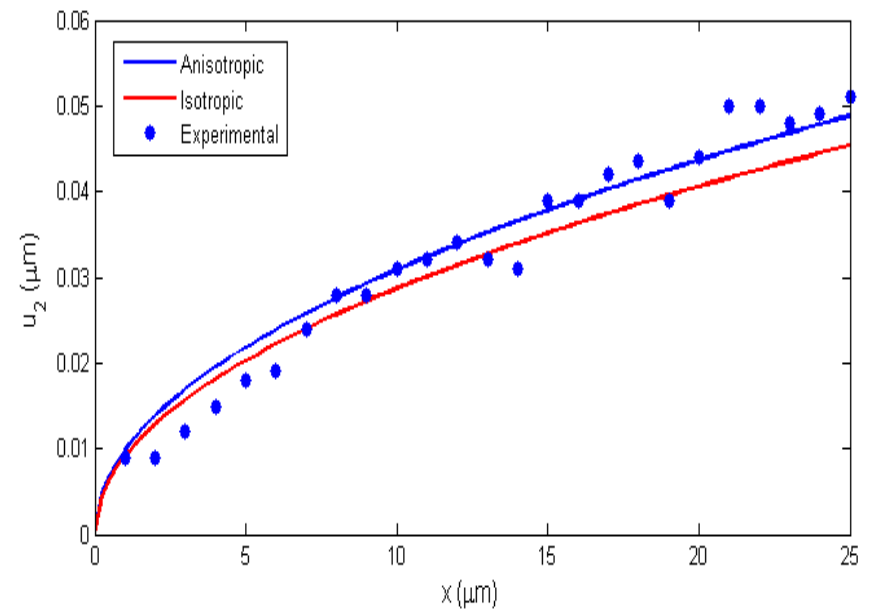
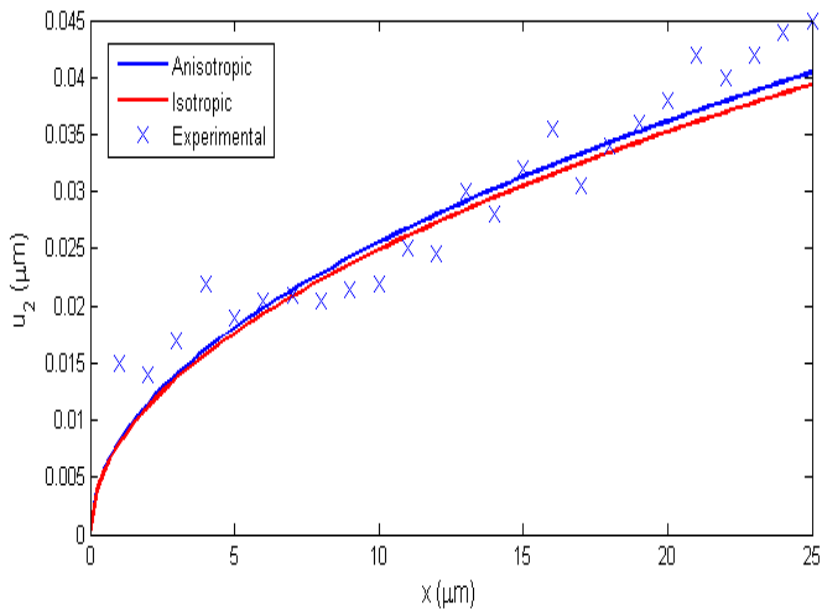
SEM Characterization

- Fracture characterization
 - Virgin vs. laser machining
- Crack opening quantified
 - Intrinsic crack tip toughness measured



Fracture Toughness

- $K_{1c} \cong 2.3 \text{ MPa}\cdot\text{m}^{1/2}$
- $G_c \cong 11.65 \text{ N/m}$



Federal Aviation
Administration

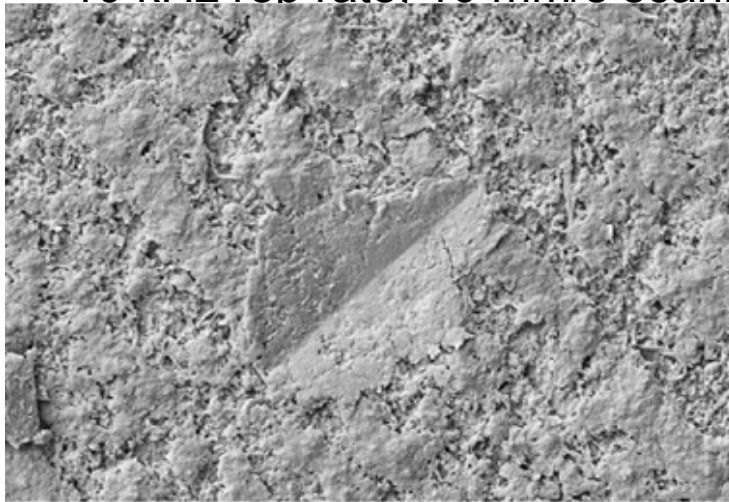
Annual Technical Meeting (ATM3)



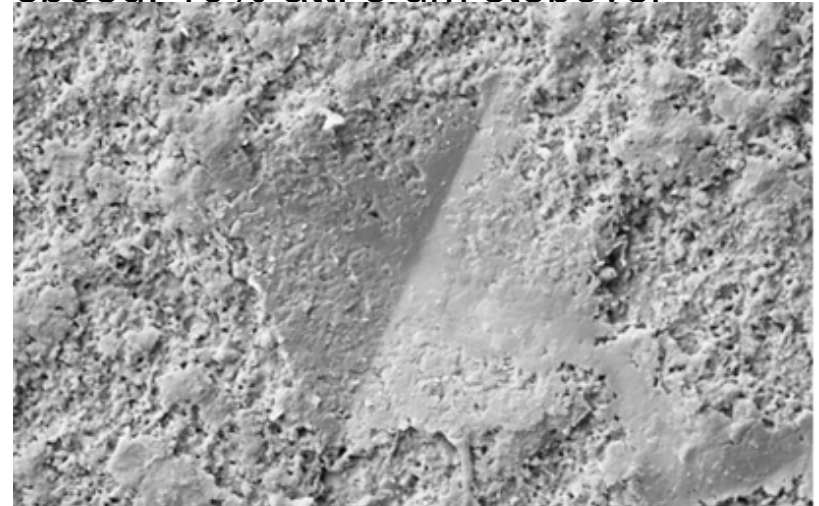
or
transportation

Toughness Induced Laser Machining

- Preliminary Vicker's indentation characterization
- No visible cracks
- Laser machining parameters
 - 10 kHz rep rate, 10 mm/s scanning speed, 10% att, 3 um stepover



12 um



12um



Federal Aviation
Administration

al Technical Meeting (ATM3)



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Summary

- Correlated crystal structure with anisotropic elastic properties
- Quantified crack tip toughness in virgin sapphire specimens
 - Good correlation with data in literature
- Laser machining effects on fracture
 - Unusual toughness enhancement
- Hypothesis: Laser induced dislocations
 - TEM characterization and dislocation/fracture modeling currently underway



Acknowledgements

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- FAA
- FAMU-FSU College of Engineering
- University of Florida
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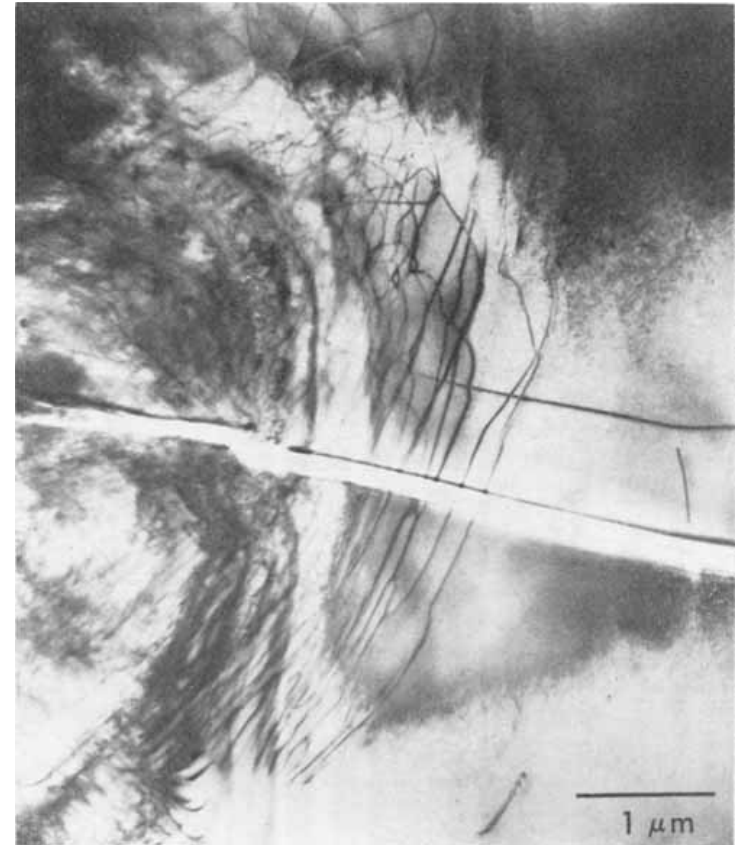
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Dislocation Mechanics

- Basal dislocations associated with a 100-g indentation on a (0001) basal plane section
- Specimen polished with abrasive paper.
- How does this influenced by laser machining?



Background

- Brittle
- Extremely hard material
 - Ranks a 9 on the Mohs scale
- Melting temperature of 2030°C
- Chemically inert



Introduction

- Crystallographic Structure
 - Hexagonal
 - Rhombohedral

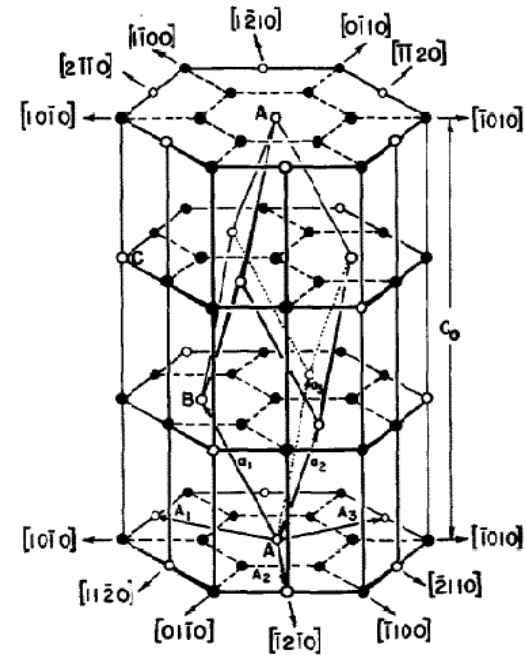


Table 4. Determined elastic constants of corundum and their standard deviations in GPa. Previous data are also shown

C_{11}	C_{33}	C_{44}	C_{12}	C_{13}	C_{14}	Ref.
496.9 ± 1.4	500.5 ± 1.6	146.8 ± 0.2	162.3 ± 1.6	115.5 ± 1.6	-21.9 ± 0.2	present work
496	502	141	135	117	-23	[8]
496.8 ± 1.8	498.1 ± 1.4	147.4 ± 0.2	163.6 ± 1.8	110.9 ± 2.2	-23.5 ± 0.3	[9]
490.2	490.2	145.4	165.4	113.0	-23.2	[10]
497.4	499.4	147.4	164.0	112.3	-23.6	[11]
497.60 ± 0.18	501.85 ± 0.21	147.24 ± 0.13	162.6 ± 0.4	117.18 ± 0.19	-22.90 ± 0.11	[12]

Current Work

- Using Stroh's Formulism for 2D anisotropic elastic body.

Stress-strain law $\sigma_{ij} = C_{ijks} u_{k,s}$

Equation of Equilibrium $C_{ijks} u_{k,sj} = 0$

Let $u_i = a_i f(z)$

Assume Solution $z = x_1 + p x_2$

$$(C_{11} k_1 + p(C_{i1} k_2 + C_{i2} k_1) + p^2 C_{i2} k_2) a_k = 0$$

